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# MA3201 - PROBLEM SHEET 5

## FALL 2008

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The problem session will be on Thursday November 6th in F3.

**Left from last time:** Problems 2 and 5 from the Midterm Exam of 2007.

**Problem 1.** Let  $R_1, R_2$  be rings and  $R = R_1 \times R_2$ .

- Show that the left ideals in  $R_1 \times R_2$  are of the form  $I_1 \times I_2$ , where  $I_1$  is an ideal in  $R_1$  and  $I_2$  is an ideal in  $R_2$ .
- Show that  $I$  is nilpotent in  $R$  if and only if  $I_1$  is nilpotent in  $R_1$  and  $I_2$  is nilpotent in  $R_2$ .
- Show that  $R$  is left artinian if and only if  $R_1$  and  $R_2$  are left artinian.

**Problem from the book:** Problem 1 on p. 401.

**Exam problems:**

Exam	Problem numbers
MA3201 11/12 -07	1*, 2*, 3*
MNFMA318 7/12 -02	1, 2

Problems marked with \* can be handed in at the lecture Monday November 3rd.