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> with(Student[VectorCalculus]) :
> M := (x, y) -> (x - 1) / (4 + x^2 + y^2) :
> N := (x, y) -> y / (4 + x^2 + y^2) :
> KurveEn := LineInt(VectorField(⟨M(x, y), N(x, y)⟩), Path(⟨1 + cos(t), sin(t)⟩, t = 0 .. Pi)) :
> KurveTo := LineInt(VectorField(⟨M(x, y), N(x, y)⟩), Line(⟨0, 0⟩, ⟨2, 0⟩)) :
> KurveEn + KurveTo

```

$$\frac{1}{2} \ln(2) - \frac{1}{8} \pi \quad (1)$$

```

> -1/2 * (1)

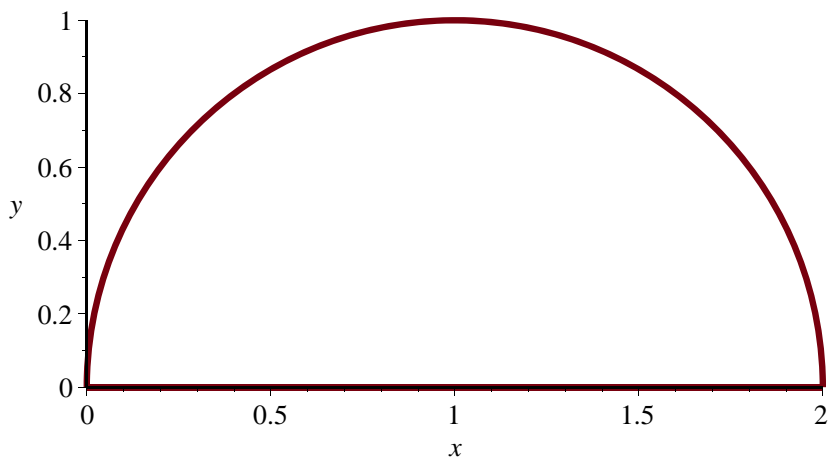
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$$-\frac{1}{4} \ln(2) + \frac{1}{16} \pi \quad (2)$$

```

> with(plots) :
> P1 := plot([1 + cos(t), sin(t), t = 0 .. Pi], thickness = 3) :
> P2 := plot([t, 0, t = 0 .. 2], thickness = 3) :
> display(P1, P2, view = [0 .. 2, 0 .. 1], scaling = constrained, labels = [x, y]);

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> with(Student[MultivariateCalculus]) :

> MultiInt  $\left( \frac{r \cdot \sin(\theta)}{(4 + r^2)^2}, r = 0 .. 2 \cdot \cos(\theta), \theta = 0 .. \frac{\pi}{2}, \text{coordinates} = \text{polar}[r, \theta], \text{output} = \text{steps} \right)$

$$\int_0^{\frac{\pi}{2}} \int_0^{2 \cos(\theta)} \frac{r^2 \sin(\theta)}{(4 + r^2)^2} dr d\theta$$

$$= \int_0^{\frac{\pi}{2}} \left( \left( -\frac{\sin(\theta) r}{2(4 + r^2)} + \frac{\sin(\theta) \arctan\left(\frac{r}{2}\right)}{4} \right) \Big|_{r=0}^{r=2 \cos(\theta)} \right) d\theta$$

$$= \int_0^{\frac{\pi}{2}} \frac{(-\cos(\theta) + \arctan(\cos(\theta)) + \arctan(\cos(\theta)) \cos(\theta)^2) \sin(\theta)}{4(\cos(\theta)^2 + 1)} d\theta$$

$$= \left( -\frac{\cos(\theta) \arctan(\cos(\theta))}{4} + \frac{\ln(\cos(\theta)^2 + 1)}{4} \right) \Big|_{\theta=0}^{\theta=\frac{\pi}{2}}$$

$$-\frac{1}{4} \ln(2) + \frac{1}{16} \pi$$

(3)