

## Survey about Lebesgue integral (Plan)

1. Lebesgue integral vs Riemann integral (idea)

2. Sets of zero measure.

3. Idea of measurable set

4. Characteristic functions

5. General pattern of construction of the  
Lebesgue integral

6. Properties of the integral (p.113)

7. Integral over a measurable set

Idea of measure. Dirac  $\delta$ -measure

8. Further properties: Linearity, monotonicity

9. Convergence theorems:

a. general theorems about convergence

b. Monotone convergence

c. Dominating convergence.

d. Fatou's lemma

10. Lebesgue integral over  $\mathbb{R}^D$  sets.

(Comments of the sets of zero measure)

11. Fubini theorem

12.  $L^p$  spaces.