

# TMA4265 Stochastic Processes

## Week 38 – Exercises

### Exercises from the book

4.10, 4.16

### Exercise 1

Given a homogeneous Markov chain, where the transition matrix  $\mathbf{P}$  depends on a parameter  $p$  given by

$$\mathbf{P} = \begin{array}{c} \begin{array}{cccc} & 1 & 2 & 3 & 4 \\ \begin{array}{l} 1 \\ 2 \\ 3 \\ 4 \end{array} & \begin{pmatrix} 0.2 & p & 0 & 0.8-p \\ 0.3 & 0.7 & 0 & 0 \\ 0 & 0.1 & 0.1 & 0.8 \\ 0.1 & p & 0.1 & 0.8-p \end{pmatrix} \end{array} \end{array}$$

For which value of  $p$  is the Markov chain not irreducible?

### Exercise 2

Consider a Markov chain whose transition probability matrix is given by

$$\mathbf{P} = \begin{array}{c} \begin{array}{cccc} & 0 & 1 & 2 & 3 \\ \begin{array}{l} 0 \\ 1 \\ 2 \\ 3 \end{array} & \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0.1 & 0.4 & 0.1 & 0.4 \\ 0.2 & 0.1 & 0.6 & 0.1 \\ 0 & 0 & 0 & 1 \end{pmatrix} \end{array} \end{array}$$

- Starting in state 1, determine the probability that the Markov chain ends in state 0.
- Determine the mean time of absorption given the process starts in state 1.