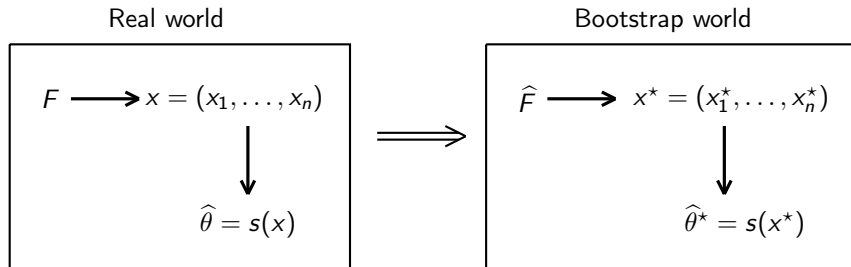


## Plug-in principle and bootstrapping

- ★ Assume: Have observed  $x_1, \dots, x_n$  iid from  $F$
- ★ Empirical distribution  $\hat{F}$  puts probability  $\frac{1}{n}$  on each  $x_1, \dots, x_n$
- ★ Parameter of interest:  $\theta = t(F)$
- ★ Plug-in principle:  $\hat{\theta} = t(\hat{F})$
- ★ Bootstrapping: Schematic view



## Bootstrapping of standard error

- ★ Have  $F \rightarrow x = (x_1, \dots, x_n)$
- ★ Empirical distribution  $\hat{F}$
- ★ Parameter of interest:  $\theta = t(F)$
- ★ Estimator:  $\hat{\theta} = s(x)$
- ★ Want to estimate  $SD_F [\hat{\theta}]$
- ★ Ideal bootstrap estimator:  $SD_{\hat{F}} [\hat{\theta}^*]$
- ★ Pseudo code for bootstrap estimator  $\widehat{SE}_B$ 
  - for**  $b = 1, 2, \dots, B$  **do**
  - Generate  $x^{*b} = (x_1^{*b}, \dots, x_n^{*b})$
  - Evaluate  $\hat{\theta}^*(b) = s(x^{*b})$
  - end for**
  - Estimate  $SD_{\hat{F}} [\hat{\theta}^*]$  by

$$\widehat{SE}_B = \sqrt{\frac{1}{B-1} \sum_{b=1}^B \left( \hat{\theta}^*(b) - \hat{\theta}^*(\cdot) \right)^2}$$