

3.

	$n = 5$	$n = 10$	$n = 100$	$n = 1000$
Solve $Ax = b$ by Gauss-Jordan elimination	+ : 50 x : 65	+ : 375 x : 430	+ : 383,250 x : 343,300	+ : 333,283,500 x : 334,333,000
Solve $Ax = b$ by Gaussian elimination	+ : 50 x : 65	+ : 375 x : 430	+ : 383,250 x : 343,300	+ : 333,283,500 x : 334,333,000
Find A^{-1} by reducing $[A \mid I]$ to $[I \mid A^{-1}]$	+ : 80 x : 125	+ : 810 x : 1000	+ : 980,100 x : 1,000,000	+ : 998,001,000 x : 1,000,000,000
Solve $Ax = b$ as $x = A^{-1}b$	+ : 100 x : 150	+ : 900 x : 1100	+ : 990,000 x : 1,010,000	+ : 999,000,000 x : 1,001,000,000
Find $\det(A)$ by row reduction	+ : 30 x : 44	+ : 285 x : 339	+ : 328,350 x : 333,399	+ : 332,833,500 x : 333,333,999
Solve $Ax = b$ by Cramer's Rule	+ : 180 x : 264	+ : 3135 x : 3729	+ : 33,163,350 x : 33,673,399	+ : 33,316,633 $\times 10^4$ x : 33,366,733 $\times 10^4$

4.

	$n = 5$	$n = 10$	$n = 100$	$n = 1000$
Solve $Ax = b$ by Gauss-Jordan elimination	Execution Time (sec) 1.55×10^{-4}	Execution Time (sec) 1.05×10^{-3}	Execution Time (sec) .878	Execution Time (sec) 836
Solve $Ax = b$ by Gaussian elimination	Execution Time (sec) 1.55×10^{-4}	Execution Time (sec) 1.05×10^{-3}	Execution Time (sec) .878	Execution Time (sec) 836
Find A^{-1} by reducing $[A \mid I]$ to $[I \mid A^{-1}]$	Execution Time (sec) 2.84×10^{-4}	Execution Time (sec) 2.41×10^{-3}	Execution Time (sec) 2.49	Execution Time (sec) 2499
Solve $Ax = b$ as $x = A^{-1}b$	Execution Time (sec) 3.50×10^{-4}	Execution Time (sec) 2.65×10^{-3}	Execution Time (sec) 2.52	Execution Time (sec) 2502
Find $\det(A)$ by row reduction	Execution Time (sec) 1.03×10^{-4}	Execution Time (sec) 8.21×10^{-4}	Execution Time (sec) .831	Execution Time (sec) 833
Solve $Ax = b$ by Cramer's Rule	Execution Time (sec) 6.18×10^{-4}	Execution Time (sec) 90.3×10^{-4}	Execution Time (sec) 83.9	Execution Time (sec) 834×10^3

Exercise Set 9.9
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1. $x_1 = 2, x_2 = 1$ 3. $x_1 = 3, x_2 = -1$ 5. $x_1 = -1, x_2 = 1, x_3 = 0$
 7. $x_1 = -1, x_2 = 1, x_3 = 0$ 9. $x_1 = -3, x_2 = 1, x_3 = 2, x_4 = 1$

11. (a) $A = LU = \begin{bmatrix} 2 & 0 & 0 \\ -2 & 1 & 0 \\ 2 & 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & \frac{1}{2} & -\frac{1}{2} \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}$

(b) $A = L_1DU = \begin{bmatrix} 1 & 0 & 0 \\ -1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 2 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & \frac{1}{2} & -\frac{1}{2} \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}$

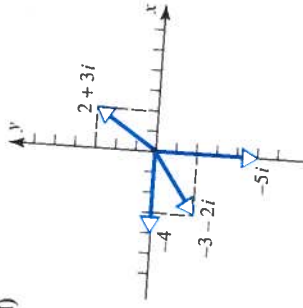
(c) $A = L_2U_2 = \begin{bmatrix} 1 & 0 & 0 \\ -1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 2 & 1 & -1 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}$

13. (b) $\begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ c & 1 \end{bmatrix} \begin{bmatrix} a & b \\ 0 & ad-bc \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & \frac{1}{a} \end{bmatrix}$

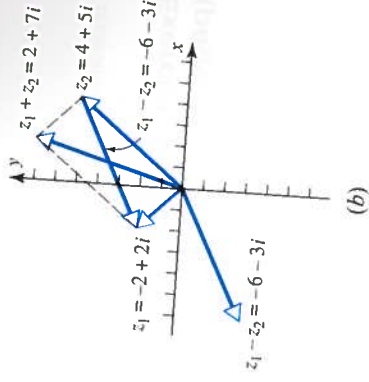
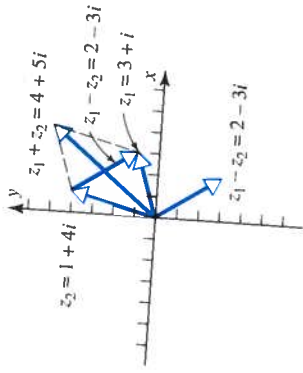
18. $A = PLU = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} 3 & 0 & 0 \\ 0 & 2 & 0 \\ 3 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & -\frac{1}{3} & 0 \\ 0 & 1 & \frac{1}{2} \\ 0 & 0 & 1 \end{bmatrix}$

Exercise Set 10.1
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1. (a-d)



3. (a) $x = -2, y = -3$ (b) $x = 2, y = 1$
 5. (a) $2 + 3i$ (b) $-1 - 2i$ (c) $-2 + 9i$
 6.



9. (a) $z_1z_2 = 3 + 3i, z_1^2 = -9, z_2^2 = -2i$
 (b) $z_1z_2 = 26, z_1^2 = -20 + 48i, z_2^2 = -5 - 12i$
 (c) $z_1z_2 = \frac{11}{3} - i, z_1^2 = \frac{1}{9}(-3 + 4i), z_2^2 = -6 - \frac{5}{2}i$

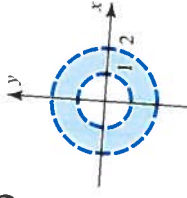
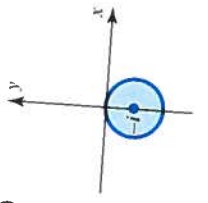
11. $76 - 88i$ 12. $26 - 18i$ 16. $(2 + \sqrt{2}) + i(1 - \sqrt{2})$ 18. $-24i$

20. (a) $\begin{bmatrix} 13 + 13i & -8 + 12i & -33 - 22i \\ 1 + i & 0 & i \\ 7 + 9i & -6 + 6i & -16 - 16i \end{bmatrix}$ (b) $\begin{bmatrix} 6 + 2i & -11 + 19i \\ -1 + 6i & -9 - 5i \end{bmatrix}$

(c) $\begin{bmatrix} 6i & 1 + i \\ -6 - i & 5 - 9i \end{bmatrix}$ (d) $\begin{bmatrix} 22 - 7i & 2 + 10i \\ -5 - 4i & 6 - 8i \end{bmatrix}$

22. (a) $z = -1 \pm i$ (b) $z = \frac{1}{2} \pm \frac{\sqrt{3}}{2}i$

1. (a) $2 - 7i$ (b) $-3 + 5i$ (c) $-5i$ (d) i (e) -9 (f) 0
 5. (a) $-i$ (b) $\frac{1}{26} + \frac{5}{26}i$ (c) $7i$ 7. $\frac{1}{2} + \frac{1}{2}i$ 9. $-\frac{7}{625} - \frac{24}{625}i$
 11. $\frac{1-\sqrt{3}}{4} + \frac{1+\sqrt{3}}{4}i$ 15. (a) $-1 - 2i$ (b) $-\frac{3}{25} - \frac{4}{25}i$
 18. (a)



Exercise Set 10.2
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