$f(x_{1:6}|y_{1:3}) = cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6)$

 $f(x_{1:6}|y_{1:3}) = cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6)$ $f(x_{2:6}|y_{1:3}) =$

$$f(x_{1:6}|y_{1:3}) = cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6)$$

$$f(x_{2:6}|y_{1:3}) = c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6)$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \end{aligned}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \end{aligned}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3:6}|y_{1:3}) &= c\left[\sum_{x_2}\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) \end{aligned}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3:6}|y_{1:3}) &= c\left[\sum_{x_2}\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{345}(x_3, x_4, x_5)g_{36}(x_3, x_6) \end{aligned}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3:6}|y_{1:3}) &= c\left[\sum_{x_2}\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{345}(x_3, x_4, x_5)g_{36}(x_3, x_6) \\ f(x_{4:6}|y_{1:3}) &= c\sum_{x_3}\widetilde{g}_{345}(x_3, x_4, x_5)g_{36}(x_3, x_6) \end{aligned}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3:6}|y_{1:3}) &= c\left[\sum_{x_2}\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{345}(x_3, x_4, x_5)g_{36}(x_3, x_6) \\ f(x_{4:6}|y_{1:3}) &= c\sum_{x_3}\widetilde{g}_{345}(x_3, x_4, x_5)g_{36}(x_3, x_6) = c\widetilde{g}_{456}(x_4, x_5, x_6) \end{aligned}$$

$$\begin{split} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3:6}|y_{1:3}) &= c\left[\sum_{x_2}\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{345}(x_3, x_4, x_5)g_{36}(x_3, x_6) \\ f(x_{4:6}|y_{1:3}) &= c\sum_{x_3}\widetilde{g}_{345}(x_3, x_4, x_5)g_{36}(x_3, x_6) \\ f(x_{56}|y_{1:3}) &= c\sum_{x_4}\widetilde{g}_{456}(x_4, x_5, x_6) \\ &= \widetilde{g}_{56}(x_5, x_6) \end{split}$$

$$\begin{split} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3:6}|y_{1:3}) &= c\left[\sum_{x_2}\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{345}(x_3, x_4, x_5)g_{36}(x_3, x_6) \\ f(x_{4:6}|y_{1:3}) &= c\sum_{x_3}\widetilde{g}_{345}(x_3, x_4, x_5)g_{36}(x_3, x_6) \\ f(x_{56}|y_{1:3}) &= c\sum_{x_4}\widetilde{g}_{56}(x_4, x_5, x_6) \\ &= \widetilde{g}_{56}(x_5, x_6) \\ f(x_6|y_{1:3}) &= c\sum_{x_5}\widetilde{g}_{56}(x_5, x_6) \\ &= \widetilde{g}_{56}(x_6) \end{split}$$

$$\begin{split} f(\mathbf{x}_{1:6}|\mathbf{y}_{1:3}) &= cg_{12}(\mathbf{x}_1, \mathbf{x}_2)g_{245}(\mathbf{x}_2, \mathbf{x}_4, \mathbf{x}_5)g_{235}(\mathbf{x}_2, \mathbf{x}_3, \mathbf{x}_5)g_{36}(\mathbf{x}_3, \mathbf{x}_6) \\ f(\mathbf{x}_{2:6}|\mathbf{y}_{1:3}) &= c\left[\sum_{\mathbf{x}_1} g_{12}(\mathbf{x}_1, \mathbf{x}_2)\right]g_{245}(\mathbf{x}_2, \mathbf{x}_4, \mathbf{x}_5)g_{235}(\mathbf{x}_2, \mathbf{x}_3, \mathbf{x}_5)g_{36}(\mathbf{x}_3, \mathbf{x}_6) \\ &= ch_2(\mathbf{x}_2)g_{245}(\mathbf{x}_2, \mathbf{x}_4, \mathbf{x}_5)g_{235}(\mathbf{x}_2, \mathbf{x}_3, \mathbf{x}_5)g_{36}(\mathbf{x}_3, \mathbf{x}_6) \\ &= c\widetilde{g}_{245}(\mathbf{x}_2, \mathbf{x}_4, \mathbf{x}_5)g_{235}(\mathbf{x}_2, \mathbf{x}_3, \mathbf{x}_5)g_{36}(\mathbf{x}_3, \mathbf{x}_6) \\ f(\mathbf{x}_{3:6}|\mathbf{y}_{1:3}) &= c\left[\sum_{\mathbf{x}_2} \widetilde{g}_{245}(\mathbf{x}_2, \mathbf{x}_4, \mathbf{x}_5)g_{235}(\mathbf{x}_2, \mathbf{x}_3, \mathbf{x}_5)\right]g_{36}(\mathbf{x}_3, \mathbf{x}_6) \\ f(\mathbf{x}_{4:6}|\mathbf{y}_{1:3}) &= c\sum_{\mathbf{x}_3} \widetilde{g}_{345}(\mathbf{x}_3, \mathbf{x}_4, \mathbf{x}_5)g_{36}(\mathbf{x}_3, \mathbf{x}_6) \\ f(\mathbf{x}_{56}|\mathbf{y}_{1:3}) &= c\sum_{\mathbf{x}_4} \widetilde{g}_{456}(\mathbf{x}_4, \mathbf{x}_5, \mathbf{x}_6) \\ f(\mathbf{x}_6|\mathbf{y}_{1:3}) &= c\sum_{\mathbf{x}_4} \widetilde{g}_{56}(\mathbf{x}_5, \mathbf{x}_6) \\ = \widetilde{g}_{6}(\mathbf{x}_6) \\ 1 &= c\sum_{\mathbf{x}_6} \widetilde{g}_{6}(\mathbf{x}_6) \Rightarrow c = 1/\sum_{\mathbf{x}_6} \widetilde{g}_{6}(\mathbf{x}_6) \end{split}$$

 $f(x_{1:6}|y_{1:3}) = cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6)$

$$f(x_{1:6}|y_{1:3}) = cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6)$$

$$f(x_{2:6}|y_{1:3}) =$$

$$f(x_{1:6}|y_{1:3}) = cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6)$$

$$f(x_{2:6}|y_{1:3}) = c\left[\sum_{x_1} g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6)$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \end{aligned}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \end{aligned}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:3,5:6}|y_{1:3}) &= c\left[\sum_{x_4}\widetilde{g}_{245}(x_2, x_4, x_5)\right]g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \end{aligned}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\tilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:3,5:6}|y_{1:3}) &= c\left[\sum_{x_4}\tilde{g}_{245}(x_2, x_4, x_5)\right]g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_{25}(x_2, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \end{aligned}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:3,5:6}|y_{1:3}) &= c\left[\sum_{x_4}\widetilde{g}_{245}(x_2, x_4, x_5)\right]g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_{25}(x_2, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \end{aligned}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1} g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:3,5:6}|y_{1:3}) &= c\left[\sum_{x_4} \widetilde{g}_{245}(x_2, x_4, x_5)\right]g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_{25}(x_2, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3,5:6}|y_{1:3}) &= c\left[\sum_{x_2} \widetilde{g}_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) \end{aligned}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1} g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:3,5:6}|y_{1:3}) &= c\left[\sum_{x_4} \widetilde{g}_{245}(x_2, x_4, x_5)\right]g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_{25}(x_2, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3,5:6}|y_{1:3}) &= c\left[\sum_{x_2} \widetilde{g}_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{35}(x_3, x_5)g_{36}(x_3, x_6) \\ \end{aligned}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1} g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\tilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:3,5:6}|y_{1:3}) &= c\left[\sum_{x_4} \tilde{g}_{245}(x_2, x_4, x_5)\right]g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\tilde{g}_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\tilde{g}_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3,5:6}|y_{1:3}) &= c\left[\sum_{x_2} \tilde{g}_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) \\ f(x_{3,6}|y_{1:3}) &= c\left[\sum_{x_5} \tilde{g}_{35}(x_3, x_5)\right]g_{36}(x_3, x_6) \end{aligned}$$

$$\begin{split} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:3,5:6}|y_{1:3}) &= c\left[\sum_{x_4}\widetilde{g}_{245}(x_2, x_4, x_5)\right]g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3,5:6}|y_{1:3}) &= c\left[\sum_{x_2}\widetilde{g}_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) = c\widetilde{g}_{35}(x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3,6}|y_{1:3}) &= c\left[\sum_{x_5}\widetilde{g}_{35}(x_3, x_5)\right]g_{36}(x_3, x_6) = ch_3(x_3)g_{36}(x_3, x_6) \\ \end{split}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1} g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:3,5:6}|y_{1:3}) &= c\left[\sum_{x_4} \widetilde{g}_{245}(x_2, x_4, x_5)\right]g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\widetilde{g}_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3,5:6}|y_{1:3}) &= c\left[\sum_{x_2} \widetilde{g}_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) = c\widetilde{g}_{35}(x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3,6}|y_{1:3}) &= c\left[\sum_{x_5} \widetilde{g}_{35}(x_3, x_5)\right]g_{36}(x_3, x_6) = ch_3(x_3)g_{36}(x_3, x_6) = c\widetilde{g}_{36}(x_3, x_6) \\ \end{array}$$

$$\begin{aligned} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\tilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:3,5:6}|y_{1:3}) &= c\left[\sum_{x_4}\tilde{g}_{245}(x_2, x_4, x_5)\right]g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_{25}(x_2, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\tilde{g}_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3,5:6}|y_{1:3}) &= c\left[\sum_{x_2}\tilde{g}_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) = c\tilde{g}_{35}(x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3,6}|y_{1:3}) &= c\left[\sum_{x_5}\tilde{g}_{35}(x_3, x_5)\right]g_{36}(x_3, x_6) = ch_3(x_3)g_{36}(x_3, x_6) = c\tilde{g}_{36}(x_5) \\ f(x_6|y_{1:3}) &= c\left[\sum_{x_5}\tilde{g}_{36}(x_3, x_6)\right] = \tilde{g}_6(x_6) \end{aligned}$$

$$\begin{split} f(x_{1:6}|y_{1:3}) &= cg_{12}(x_1, x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:6}|y_{1:3}) &= c\left[\sum_{x_1}g_{12}(x_1, x_2)\right]g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_2(x_2)g_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\tilde{g}_{245}(x_2, x_4, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{2:3,5:6}|y_{1:3}) &= c\left[\sum_{x_4}\tilde{g}_{245}(x_2, x_4, x_5)\right]g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= ch_{25}(x_2, x_5)g_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ &= c\tilde{g}_{235}(x_2, x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3,5:6}|y_{1:3}) &= c\left[\sum_{x_2}\tilde{g}_{235}(x_2, x_3, x_5)\right]g_{36}(x_3, x_6) = c\tilde{g}_{35}(x_3, x_5)g_{36}(x_3, x_6) \\ f(x_{3,6}|y_{1:3}) &= c\left[\sum_{x_5}\tilde{g}_{35}(x_3, x_5)\right]g_{36}(x_3, x_6) = ch_3(x_3)g_{36}(x_3, x_6) = c\tilde{g}_{36}(x_6) \\ f(x_6|y_{1:3}) &= c\left[\sum_{x_5}\tilde{g}_{36}(x_3, x_6)\right] = \tilde{g}_6(x_6) \Rightarrow c = 1/\sum_{x_6}\tilde{g}_6(x_6) \end{split}$$