

Complex Numbers in Polar Form

$$z = x + iy, r = |z| = \sqrt{x^2 + y^2}, x = r \cos \theta, y = r \sin \theta$$
$$\theta = \arctan(y/x) + k\pi \text{ (according to the quadrant)}$$

$$z = r(\cos \theta + i \sin \theta) = r e^{i\theta}$$

Multiplication and Division in Polar Form

$$z_1 = r_1 e^{i\theta}, z_2 = r_2 e^{i\phi}$$

$$z_1 z_2 = r_1 r_2 e^{i(\theta + \phi)}, z_1 / z_2 = r_1 / r_2 e^{i(\theta - \phi)}$$

De Moivre's Formula

$$z^n = r^n (\cos n\theta + i \sin n\theta) = r^n e^{ni\theta}$$

Roots Equation $w^n = z$ has n solutions

$$w_k = \sqrt[n]{r} (\cos(\theta/n + 2\pi k/n) + i \sin(\theta/n + 2\pi k/n)),$$
$$k = 0, 1, \dots, n-1$$

Points w_0, w_1, \dots, w_{n-1} lie on a circle of radius $\sqrt[n]{r}$ and center 0 and constitute the vertices of a regular polygon.

Quadratic Equation $z^2 + pz + q = 0,$

$$z_{1,2} = (-p \pm \sqrt{p^2 - 4q})/2$$