

TMA4155 — Exercise 5

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Task 1 — RSA encryption

You want to strengthen your RSA encryption, but you do not want to have two different modulus (because this leads to a much larger public key). So you decide to do as follows: First encrypt with the public key (n, e_1) , then with the public key (n, e_2) . Explain why this does not lead to increased security.

Task 2 — Euclid's algorithm

Use Euclid's algorithm to compute $\gcd(a, b)$ for:

- a. $a = 153, b = 157$.
- b. $a = 153, b = 187$.
- c. $a = 10005, b = 1101$.
- d. $a = 10005, b = 1103$.

Task 3 — Modular inverses

Use the extended Euklid's algorithm to find an inverse for a modulo n for:

- a. $a = 153, n = 157$.
- b. $a = 157, n = 153$.
- c. $a = 1103, n = 10005$.
- d. $a = 73, n = 1103$.

Task 4 — Primality testing

Compute 2^{560} , 5^{560} and 7^{560} modulo 561. What would the Fermat test say about 561 being prime?