

$\vec{x}(t) = f(\vec{x}, t)$
 UNIQUE SOLUTIONS

$\vec{x}^*(t)$ SOLUTION WITH $\vec{x}^*(t_0) = \vec{a}$

$$\Downarrow \forall \epsilon > 0 \exists \delta > 0 \text{ ST } \|\vec{x}^*(t_0) - \vec{x}(t_0)\| < \delta \Rightarrow \|\vec{x}^*(t) - \vec{x}(t)\| < \epsilon \quad \forall t \geq t_0.$$

$\vec{x}^*(t)$ LIAPUNOV STABLE FOR $t \geq t_0$

$$\Downarrow \delta \text{ ABOVE ONLY DEPENDENT ON } \epsilon, \text{ BUT NOT ON } t_0.$$

$\vec{x}^*(t)$ UNIFORMLY STABLE FOR $t \geq t_0$

$$\Downarrow \exists \eta(t_0) > 0 \text{ ST } \|\vec{x}(t_0) - \vec{x}^*(t_0)\| < \eta \Rightarrow \lim_{t \rightarrow \infty} \|\vec{x}(t) - \vec{x}^*(t)\| = 0$$

$\vec{x}^*(t)$ UNIFORMLY ASYMPTOTICALLY STABLE

$\vec{x}^*(t)$ LIAPUNOV STABLE FOR $t \geq t_0$

$$\Downarrow \exists \eta(t_0) > 0 \text{ ST } \|\vec{x}(t_0) - \vec{x}^*(t_0)\| < \eta \Rightarrow \lim_{t \rightarrow t_0} \|\vec{x}(t) - \vec{x}^*(t_0)\| = 0$$

$\vec{x}^*(t)$ ASYMPTOTICALLY STABLE