

$$\dot{\vec{x}} = A\vec{x}$$

$\forall$ SOLUTIONS
 BOUNDED
 AS $t \rightarrow \infty$

$\operatorname{Re}(\lambda_i) < 0$
 $\forall$ EIGENVALUES λ_i

$\forall$ SOLUTIONS
 UNIFORMLY
 STABLE

$\forall$ SOLUTIONS
 ASYMPTOTICALLY
 STABLE

$C(t)$ CONT
 $\int_0^\infty \|G(s)\| ds < \infty$

$\lim_{\|\vec{x}\| \rightarrow 0} \frac{\|R(\vec{x}, t)\|}{\|\vec{x}\|} = 0$ (UNIFORM IN t)

$\forall$ SOLUTIONS
 TO $\dot{\vec{x}} = A\vec{x} + C(t)\vec{x}$
 LAPUNOV STABLE

$\forall$ SOLUTIONS
 TO $\dot{\vec{x}} = A\vec{x} + C(t)\vec{x}$
 ASYMPTOTICALLY
 STABLE

$\vec{x}(t) = \vec{0}$
 ASYMPTOTICALLY
 STABLE SOLUTION
 TO
 $\dot{\vec{x}} = A\vec{x} + R(\vec{x}, t)$

$R(\vec{x}, t) = R(\vec{x})$

RELATED TO
 LINEARIZATIONS

$$\dot{x} = f(x,y)$$

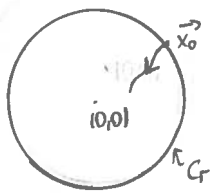
$$\dot{y} = g(x,y)$$

$(0,0)$... EQUILIBRIUM POINT

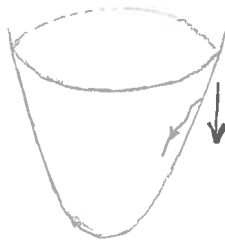
C_r ... CIRCLE: RADIUS r
CENTRE $(0,0)$

$\mathcal{H}_{\vec{x}_0}$... HALF-PATH STARTING IN $\vec{x}_0$

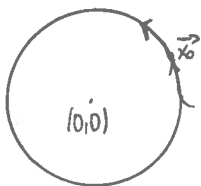
1.)



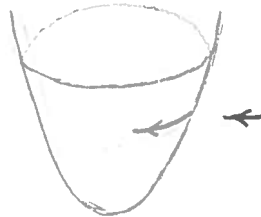
$$V(x,y) = x^2 + y^2$$



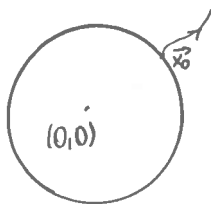
2.)



$$V(x,y) = x^2 + y^2$$



3.)



$$V(x,y) = x^2 + y^2$$

