

$$\dot{x} = f(x, y)$$

$$\dot{y} = g(x, y)$$

(x_0, y_0) EQUILIBRIUM POINT

$$I_{(x_0, y_0)} = I_M \quad (M \text{ SMOOTH SIMPLE } \odot \text{ ONLY EP SURROUNDING } (x_0, y_0))$$

$$\begin{aligned} & \Downarrow (x_i, y_i) \in \text{int } M \quad i=1, \dots, n \\ & \quad \text{(EQUILIBRIUM POINTS)} \\ I_M &= \sum_{i=1}^n I_{(x_i, y_i)} \end{aligned}$$

GENERAL:

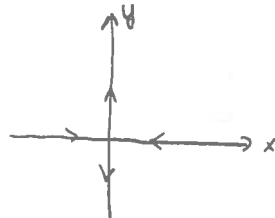
$$\uparrow \rightsquigarrow \rightarrow \rightsquigarrow \downarrow = -\pi$$

$$\downarrow \rightsquigarrow \leftarrow \rightsquigarrow \uparrow = -\pi$$

$$\uparrow \rightsquigarrow \leftarrow \rightsquigarrow \downarrow = \pi$$

$$\downarrow \rightsquigarrow \rightarrow \rightsquigarrow \uparrow = \pi$$

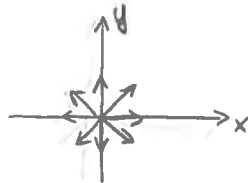
1) SADDLE



$$\uparrow \rightsquigarrow \rightarrow \rightsquigarrow \downarrow \rightsquigarrow \leftarrow = -2\pi$$

$$I_{(0,0)} = -1$$

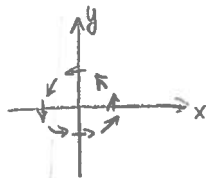
2) NODE



$$\uparrow \rightsquigarrow \leftarrow \rightsquigarrow \downarrow \rightsquigarrow \rightarrow = 2\pi$$

$$I_{(0,0)} = 1$$

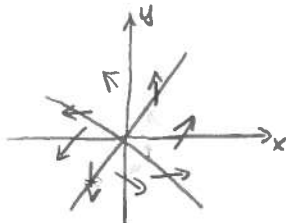
3) CENTRE



$$\uparrow \rightsquigarrow \leftarrow \rightsquigarrow \downarrow \rightsquigarrow \rightarrow = 2\pi$$

$$I_{(0,0)} = 1$$

4) SPIRAL

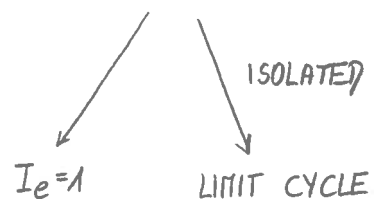


$$\uparrow \rightsquigarrow \leftarrow \rightsquigarrow \downarrow \rightsquigarrow \rightarrow = 2\pi$$

$$I_{(0,0)} = 1$$

$$\begin{aligned}\dot{x} &= f(x,y) \\ \dot{y} &= g(x,y)\end{aligned}$$

PERIODIC SOLUTIONS $\triangleq$ CLOSED PHASE PATHS C



C SIMPLE CLOSED CURVE

