

1. (Gelfand-Mazur theorem) If A is a Banach algebra in which every nonzero element is invertible, then A is isometrically isomorphic to the complex field. (*Hint:* Use the fact that the spectrum of every element in A is non-empty.)