

Chapter 10

- Two samples X_1, \dots, X_n and Y_1, \dots, Y_m (from normal populations or n and m are large enough); $\text{Var}(X_i) = \sigma_X^2$, $\text{Var}(Y_i) = \sigma_Y^2$. Testing $H_0 : \sigma_X^2 = \sigma_Y^2$. Alternatives a) $H_1 : \sigma_X^2 > \sigma_Y^2$, b) $H_1 : \sigma_X^2 < \sigma_Y^2$, c) $H_1 : \sigma_X^2 \neq \sigma_Y^2$. The level of significance α .

The test statistic

$$F = \frac{S_X^2}{S_Y^2}.$$

Critical region: a) $F \geq f_{\alpha, n-1, m-1}$, b) $F \leq f_{1-\alpha, n-1, m-1}$, a) $F \geq f_{\alpha/2, n-1, m-1}$ or $F \leq f_{1-\alpha/2, n-1, m-1}$

- P -value is the minimal level of significance such that H_0 is rejected for the observed data.

- Goodness-of-fit test. k cells, e_i are expected frequencies, o_i are observed frequencies, $i = 1, \dots, k$. The test statistic

$$\chi^2 = \sum_{i=1}^k \frac{(o_i - e_i)^2}{e_i}.$$

The critical region: $\chi^2 \geq \chi_{\alpha, k-1}^2$.

- Test for independence (categorical data: $r \times c$ contingency table). The test statistic

$$\chi^2 = \sum_{j=1}^c \sum_{i=1}^r \frac{(o_{ij} - e_{ij})^2}{e_{ij}}.$$

The critical region: $\chi^2 \geq \chi_{\alpha, (r-1)(c-1)}^2$.

The same test statistic and critical region are used for testing homogeneity.

Chapter 11

- Simple linear regression

$$Y = \beta_0 + \beta_1 x + \epsilon,$$

x is regressor (predictor, independent variable, explanatory variable), Y is response (dependent variable), ϵ is error (random variable), $E\epsilon = 0$; β_0 (intercept) and β_1 (slope) are parameters of interest.

- Data: $(x_1, Y_1), (x_2, Y_2), \dots, (x_n, Y_n)$,

$$Y_i = \beta_0 + \beta_1 x_i + \epsilon_i$$

where $\epsilon_1, \epsilon_2, \dots, \epsilon_n$ are independent normally distributed, $E\epsilon_i = 0$, $\text{Var}(\epsilon_i) = \sigma^2$.