

## Exponential Class of distributions

$$f(x|\boldsymbol{\theta}) = h(x)c(\boldsymbol{\theta})e^{\sum_{i=1}^k w_i(\boldsymbol{\theta})t_i(x)}$$

$$E\left(\sum_{i=1}^k \frac{\partial w_i(\boldsymbol{\theta})}{\partial \theta_j} t_i(X)\right) = -\frac{\partial}{\partial \theta_j} \log c(\boldsymbol{\theta})$$

$$\text{Var}\left(\sum_{i=1}^k \frac{\partial w_i(\boldsymbol{\theta})}{\partial \theta_j} t_i(X)\right) = -\frac{\partial^2}{\partial \theta_j^2} \log c(\boldsymbol{\theta}) - E\left(\sum_{i=1}^k \frac{\partial^2 w_i(\boldsymbol{\theta})}{\partial^2 \theta_j} t_i(X)\right)$$

## Location – Scale Families

$f(x)$  pdf. The family of pdfs:  $\frac{1}{\sigma} f\left(\frac{x-u}{\sigma}\right)$ ,

$$\mu \in (-\infty, \infty), \sigma > 0$$

The distribution of  $Y = \mu + \sigma X$

## Chebyshevs

$$g(x) \geq 0, r > 0$$

$$P(g(X) \geq r) \leq \frac{Eg(X)}{r}$$