

Repetition week 43

Invariance principle:

If $\hat{\theta}$ is the MLE of θ , $\tau(\hat{\theta})$ is the MLE of $\tau(\theta)$.

Bayes estimation:

Prior: $\pi(\theta)$ Posterior: $\pi(\theta|\mathbf{x})$

$$\pi(\theta|\mathbf{x}) = \frac{f(\mathbf{x}, \theta)}{f(\mathbf{x})} = \frac{f(\mathbf{x}|\theta)\pi(\theta)}{\int f(\mathbf{x}, \theta)d\theta}$$

$$\hat{\theta}_B = E(\theta|\mathbf{x})$$

The mean square error

$$MSE = E[(W - \theta)^2] = Var[W] + (E[W] - \theta)^2$$