

H9: Summing up the GWOT course

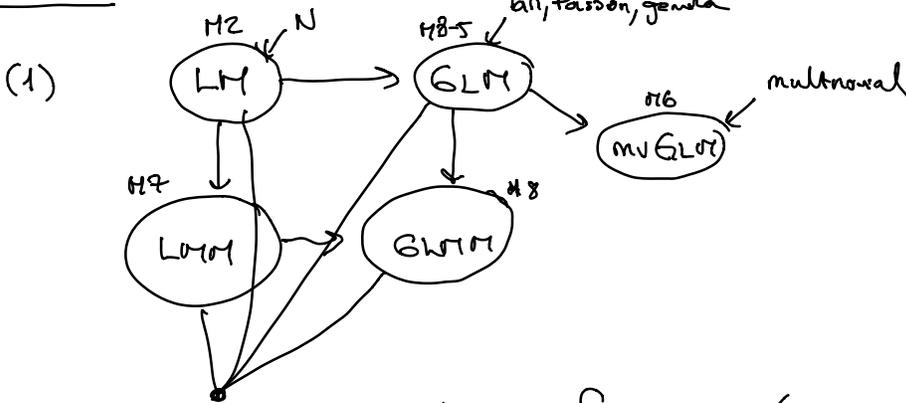
THA4015  
22.11.2018

CORE: What is the effect of covariates  $x$  on response(s)  $y$ ?

interpretation

How to predict  $y$  from  $x$ ?

BASIC 5



(c) univariate exponential family:  $f(y_i) = \exp\left(\frac{y_i \theta_i - b(\theta_i)}{\phi} \cdot w_i + c(y_i, w_i, \phi)\right)$

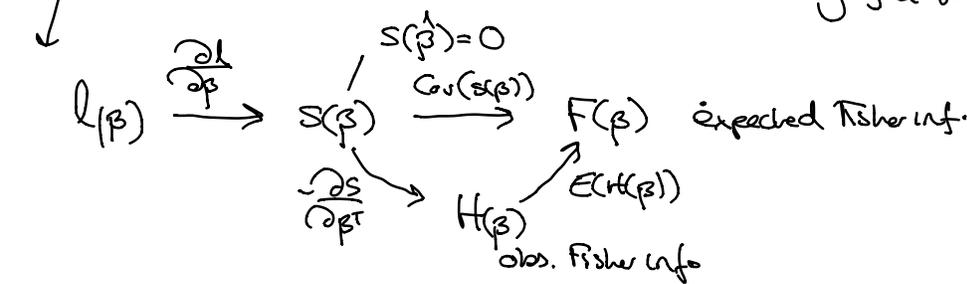
(actually mvGLM)

(2) Likelihood  $L(\beta) = \prod_{i=1}^n f(y_i)$  ← mostly for GLM

but also for LMM ~ mvN

but for GLMM  $f(y_i)$  marginal  
need  $\int f(y_i | x_i) f(x_i) dx_i$

find  $\hat{\beta}$  by maximizing the likelihood



$$\beta^{(t+1)} = \beta^{(t)} + F^{-1}(\beta^{(t)}) S(\beta) \quad \text{Fisher scoring} \xrightarrow{\text{exp. fun}} \text{IRWLS}$$

canonical link:  $f(\beta) = H(\beta)$

(3) Asymptotic distribution

$$\hat{\beta} \approx N_p(\beta, F^{-1}(\hat{\beta})) \quad \rightarrow \text{Wald test}$$

CI

$$\text{LRT} = -2 (\ln L(\hat{\beta}_B) - \ln L(\hat{\beta}_A)) \sim \chi^2_{\#A - \#B}$$

$\uparrow$  small                       $\uparrow$  big model                      B nested within A

↙ Deviance: when A is saturated model

(4)

R print-out

(5)

Exam → see Pb