



Norwegian University of  
Science and Technology

Department of Mathematical Sciences

## Examination paper for TMA4315 Generalised Linear Models

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**Examination date:** 13th December 2016

**Examination time (from-to):** 09:00–13:00

**Permitted examination support material:** C. No written or handwritten examination support materials are permitted. A simple calculator is permitted.

**Other information:**

You may write your answers for this exam in English, *Norsk (bokmål og/eller nynorsk)*, or any mix of these.

**Language:** English

**Number of pages:** 1

**Number of pages enclosed:** 0

Informasjon om trykking av eksamensoppgave	
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**Problem 1** We will consider (binomial or binary) logistic regression, where we have independent observations

$$y_i \sim \text{Binomial}(n_i, p_i), \quad i = 1, \dots, n,$$

so that

$$\text{Prob}(y_i) = \binom{n_i}{y_i} p_i^{y_i} (1 - p_i)^{n_i - y_i}, \quad y_i = 0, 1, \dots, n_i.$$

The linear predictor is

$$\eta_i = \mathbf{x}_i^T \boldsymbol{\beta},$$

and

$$p_i = \frac{\exp(\eta_i)}{1 + \exp(\eta_i)}$$

or

$$\text{logit}(p_i) = \eta_i.$$

Here,  $\mathbf{x}_i$  is the vector of the  $p$  covariates for the  $i$ 'th observation  $y_i$  with size (number of trials)  $n_i$ , and  $\boldsymbol{\beta}$  is the vector of  $p$  unknown regression coefficients.

Write an introduction to logistic regression and its practical usage, for a student with a good background in statistics but no knowledge about Generalized Linear Models (GLM). Topics you may want to consider, are

- When to use it? Underlying assumptions.
- Parameter estimation, asymptotic results for the MLE, Fisher information and observed Fisher information, confidence intervals and hypothesis testing.
- Output analysis, residual plots (when its possible) and interpretation of the  $\boldsymbol{\beta}$ -coefficients.
- Deviance and its usage.